

2 0 1 2

PHYSICS

(Major)

Paper : 2.2

Full Marks : 60

Time : 2½ hours

The figures in the margin indicate full marks for the questions

1. Choose the correct option/Answer the following : 1×7=7

(a) According to the kinetic theory of gases, the r.m.s. speed of gas molecules is directly proportional to

(i) T

(ii) \sqrt{T}

(iii) T^2

✓(iv) $\frac{1}{\sqrt{T}}$

(b) What is meant by 'mean free path' of molecules in a gas? Write down Clausius expression for it.

(c) The Boyle temperature T_B for a van der Waals' gas is given by

$$(i) T_B = \frac{8a}{27Rb}$$

$$(ii) T_B = \frac{a}{Rb}$$

$$(iii) T_B = \frac{2a}{Rb}$$

$$(iv) T_B = \frac{27}{8} T_C$$

(d) Distinguish between thermal conductivity and thermometric conductivity.

(e) The first law of thermodynamics is a restatement of law of conservation of

(i) mass

(ii) momentum

(iii) energy

(iv) None of the above

(f) Which is the more effective way to increase the efficiency of a Carnot engine : to increase the source temperature T_1 or to lower the sink temperature T_2 ?

(g) State Stefan-Boltzmann law.

2. Answer the following questions : 2×4=8

- (a) Calculate the magnitude of mean free path and the collision frequency for air molecules at 0 °C and 1 atm pressure.
- (b) Show that at the critical temperature, the departure of the van der Waals' gas law from the ideal gas law $p_c V_c / T_c = R$ measures 62.5%.
- (c) 20 g of hydrogen gas at 27 °C is compressed isothermally to one-fourth of the original volume. Find the value of the work done.
- (d) Give the Gibbs-Helmholtz equation for a reversible cell. What is its significance? When is the reaction endothermic and exothermic?

3. Answer any *three* of the following questions :

5×3=15

- (a) Establish that associated energy per degree of freedom is $\frac{1}{2} kT$.
- (b) Starting from Planck's radiation formula, obtain Rayleigh-Jeans law. Explain the limitation of Rayleigh-Jeans law.
- (c) Show that $\eta = \frac{1}{3} \rho \bar{c} \lambda$, where η is the viscosity of the gas, ρ the density, \bar{c} the mean molecular velocity and λ the mean free path.

(d) Write a short note on adiabatic demagnetisation.

(e) If $H = U + pV$ represents enthalpy of a system containing gas, prove that

$$C_P - C_V = p \left(\frac{\delta V}{\delta T} \right)_P + \left(\frac{\delta U}{\delta V} \right)_T \left(\frac{\delta V}{\delta T} \right)_P \quad \checkmark$$

4. (a) Obtain the Kelvin's thermodynamical scale of temperature. 10

Or

Show that enthalpy remains constant in Joule-Thomson effect.

(b) Deduce the expression for pressure of a confined gas on the basis of kinetic theory of gases using spherical polar coordinates. 10

Or

← Deduce Planck's law of black-body radiation and obtain Stefan's law from Planck's law.

(c) Relating to Joule-Thomson effect, obtain the relation

$$\mu C_P = - \left[\frac{\delta U}{\delta P} \right]_T + \left[- \frac{\delta}{\delta P} (PV) \right]_T$$

where μ is the Joule-Thomson coefficient $\left[\mu = \left(\frac{\delta T}{\delta P} \right)_H \right]$. 10

(5)

Or

Derive the relations

$$(i) \left(\frac{\delta s}{\delta V} \right)_T = \left(\frac{\delta p}{\delta T} \right)_V$$

$$(ii) \left(\frac{\delta p}{\delta T} \right)_{\text{sat}} = \frac{L}{T(V_2 - V_1)}$$

where the symbols have their usual meanings.

5+5=10
